
fitr Documentation

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CHAPTER 1

Contents

1.1 Installation

The current PyPI release of Fitr can be installed as follows:

```
pip install fitr
```

If you want the latest version on the GitHub master branch, install as follows:

```
pip install git+https://github.com/ComputationalPsychiatry/fitr.git
```

1.2 Conceptual Overview

1.2.1 Contents

Intro to Reinforcement Learning

Coming soon...

Modelling Behavioural Data

Pre-Built Models

We have included pre-built models for the following tasks:

Task	What it tests	Reference
N-Arm Bandit	Exploration/Exploitation	[Daw2006]
2-Step Task	Model-based vs. Model-free control	[Daw2011]

References

Fitting Models to Data

Model-Fitting Methods in Fitr

Fitr implements several model-fitting methods:

Method	Function	Reference
EM with Laplace Approximation	<code>fitr.EM()</code>	[Huys2011]
Empirical Priors	<code>fitr.EmpiricalPriors()</code>	[Gershman2016]
Markov Chain Monte-Carlo (Stan)	<code>fitr.MCMC()</code>	[StanDevs]

Here, “EM” refers to Expectation-Maximization.

References

Selecting the Best Model

Fitr facilitates model-selection via Bayesian Information Criterion (BIC), Aikake Information Criterion (AIC), and Bayesian Model Selection (BMS) [Rigoux2014]. BMS is a re-implementation of `spm_BMS()` from the Statistical Parametric Mapping toolbox for MATLAB.

References

1.3 Tutorials

We have several tutorials for Fitr written in Jupyter Notebooks:

1. Introductory tutorial (EM and Bayesian Model Selection)
2. Fitting a Model with MCMC
3. Use MCMC with your own Stan Code
4. Using Multiple Model-Fitting Routines for Same Model

1.4 Contributing to Fitr

Your contributions to Fitr are welcome and encouraged. Fitr is being developed on GitHub in order to facilitate improvements by the community. However, to ensure that Fitr develops as a robust piece of software, we have several guidelines for contributions. These have been chosen to mirror those of the SciPy/NumPy project.

Contributions to Fitr should have

1. Unit tests

- It is important that Fitr functions well “out of the box,” and this requires that code implemented in Fitr is appropriately tested.
- Fitr uses Codecov.io to assess code coverage. In general, try to ensure that your new code is covered by unit tests.

- Unit tests are written in the `/tests` folder, where you can find examples of how unit tests are currently written.

2. Documentation

- New code is not of great use unless the community knows what it is for and how to use it. As such, we ask that any new functions or modifications to existing functions carry the appropriate documentation.
- If your contribution is substantial, it may be of use to write a tutorial, which are done with Jupyter Notebooks here.
- Documentation of modules, classes, and functions can be done in Docstrings, then compiled with Sphinx and autodoc.
- Documentation of Fitr code follows the SciPy/NumPy format

3. Appropriate code style

- Fitr follows the [PEP8](#) standard, and so we recommend that you run a linter to ensure that contributions adhere to this format.

1.4.1 Types of Contributions

At this early stage, we are open to any new contributions, big or small.

Many of the contribution requirements listed above were not adhered to at Fitr's inception, so even if you would like to help by correcting some of our past mistakes, this would be an important step toward Fitr's goals!

1.4.2 How to Contribute

1. Fork the GitHub repository
2. Create a new branch
3. Submit a pull request

Fitr's master branch is protected and requires Unit tests to pass, as well as 2 reviews before merging is allowed.

1.4.3 Requesting Features and Reporting Problems

Open an issue on the Fitr GitHub page, and we'll get on it as soon as possible!

1.5 Fitr API

Modules:

1.5.1 Inference

Modules:

Maximum-Likelihood Estimation

class `fitr.inference.mle.MLE(loglik_func, params, name='MLEModel')`
Maximum Likelihood parameter estimation

Attributes

- name** [str] Name of the model being fit. We suggest using the free parameters.
- loglik_func** [function] The log-likelihood function to be used for model fitting
- params** [list] List of parameters from the rlparams module
- nparams** [int] Number of free parameters in the model
- param_rng** [list] List of strings denoting the parameter ranges (see rlparams module for further details)

Methods

<code>fit(data, n_iterations=1000, opt_algorithm='BFGS')</code>	Runs model-fitting algorithm
<code>__printfitstart(self, n_iterations, algorithm, verbose)</code>	(Private) function to print optimization info to console

fit (`data, n_iterations=1000, c_limit=0.0001, opt_algorithm='L-BFGS-B', verbose=True`)
Runs the maximum a posterior model-fitting with empirical priors.

Parameters

- data** [dict] Dictionary of data from all subjects.
- n_iterations** [int] Maximum number of iterations to allow.
- c_limit** [float] Threshold at which convergence is determined
- opt_algorithm** [{‘L-BFGS-B’}] Algorithm to use for optimization. Only works at present with L-BFGS-B.
- verbose** [bool] Whether to print progress of model fitting

Returns

ModelFitResult Representation of the model fitting results

Expectation-Maximization

class `fitr.inference.em.EM(loglik_func, params, name='EMModel')`
Expectation-Maximization with the Laplace Approximation [Huys2011], [HuysEMCode].

Attributes

- name** [str] Name of the model being fit. We suggest using the free parameters.
- loglik_func** [function] The log-likelihood function to be used for model fitting
- params** [list] List of parameters from the rlparams module
- nparams** [int] Number of free parameters in the model

param_rng [list] List of strings denoting the parameter ranges (see rlparams module for further details)

prior [scipy.stats distribution] The prior distribution over parameter estimates. Here this is fixed to a multivariate normal.

mu [ndarray(shape=nparrays)] The prior mean over parameters

cov [ndarray(shape=(nparrays,nparrays))] The covariance matrix for prior over parameter estimates

Methods

fit(data, n_iterations=1000, c_limit=1, opt_algorithm='BFGS', diag=False, verbose=True)	Run the model-fitting algorithm
logposterior(x, states, actions, rewards)	Computes the log-posterior probability
group_level_estimate(param_est, hess_inv)	Updates the hyperparameters of the group-level prior
_printfitstart(self, n_iterations, c_limit, algorithm, init_grid, grid_reinit, dofull, early_stopping, verbose)	(Private) function to print optimization info to console
_printupdate(self, opt_iter, subject_i, posterior_ll, verbose)	(Private) function to print update on fit iteration to console

fit (data, n_iterations=1000, c_limit=0.001, opt_algorithm='L-BFGS-B', init_grid=False, grid_reinit=True, n_grid_points=5, n_reinit=1, dofull=True, early_stopping=True, verbose=True)
Performs maximum a posteriori estimation of subject-level parameters

Parameters

data [dict] Dictionary of data from all subjects.

n_iterations [int] Maximum number of iterations to allow.

c_limit [float] Threshold at which convergence is determined

opt_algorithm [{‘BFGS’, ‘L-BFGS-B’}] Algorithm to use for optimization

init_grid [bool] Whether to initialize the optimizer using brute force grid search. If False, will sample from normal distribution with mean 0 and standard deviation 1.

grid_reinit [bool] If optimization does not converge, whether to reinitialize with values from grid search

n_grid_points [int] Number of points along each axis to evaluate during grid-search initialization (only meaningful if init_grid is True).

n_reinit [int] Number of times to reinitialize the optimizer if not converged

dofull [bool] Whether update of the full covariance matrix of the prior should be done. If False, the covariance matrix is limited to one in which the off-diagonal elements are set to zero.

early_stopping [bool] Whether to stop the EM procedure if the log-model-evidence begins decreasing (thereby reverting to the last iteration’s results).

verbose [bool] Whether to print progress of model fitting

Returns

ModelFitResult Representation of the model fitting results

group_level_estimate (*param_est*, *hess_inv*, *dofull*, *verbose=True*)

Updates the group-level hyperparameters

Parameters

param_est [ndarray(shape=(nsubjects, nparms))] Current parameter estimates for each subject

hess_inv [ndarray(shape=(nparms, nparms, nsubjects))] Inverse Hessian matrix estimate for each subject from the iteration with highest log-posterior probability

dofull [bool] Whether update of the full covariance matrix of the prior should be done. If False, the covariance matrix is limited to one in which the off-diagonal elements are set to zero.

verbose [bool] Controls degree to which results are printed

initialize_opt (*fn=None*, *grid=False*, *Ns=None*)

Returns initial values for the optimization

Parameters

fn [function] Function over which grid search takes place

grid [bool] Whether to return initialization values from grid search

Ns [int] Number of points per axis over which to evaluate during grid search

Returns

x0 [ndarray] 1 X N vector of initial values for each parameter

logposterior (*x*, *states*, *actions*, *rewards*)

Represents the log-posterior probability function

Parameters

x [ndarray(nparms)] Array of parameters for single subject

states [ndarray(shape=[ntrials, nsteps])] Array of states encountered by subject

actions: ndarray(shape=[ntrials, nsteps]) Array of actions taken by subject

rewards [ndarray(shape=[ntrials, nsteps])] Array of rewards received by the subject.

Returns

float Log-posterior probability

Empirical Priors

class fitr.inference.empiricalpriors.**EmpiricalPriors** (*loglik_func*, *params*,
name='EmpiricalPriorsModel')

Inference procedure with empirical priors

Attributes

name [str] Name of the model being fit. We suggest using the free parameters.

loglik_func [function] The log-likelihood function to be used for model fitting

params [list] List of parameters from the rlpars module

nparams [int] Number of free parameters in the model

param_rng [list] List of strings denoting the parameter ranges (see rlparams module for further details)

Methods

fit(data, n_iterations=1000, opt_algorithm='BFGS')	Runs model-fitting algorithm
logposterior(x, states, actions, rewards)	Computes the log-posterior probability
_printfitstart(self, n_iterations, algorithm, verbose)	(Private) function to print optimization info to console
_printupdate(self, opt_iter, subject_i, posterior_ll, verbose)	(Private) function to print iteration info to console

fit (*data, n_iterations=1000, c_limit=0.001, opt_algorithm='L-BFGS-B', verbose=True*)

Runs the maximum a posterior model-fitting with empirical priors.

Parameters

data [dict] Dictionary of data from all subjects.

n_iterations [int] Maximum number of iterations to allow.

c_limit [float] Threshold at which convergence is determined

opt_algorithm [{‘L-BFGS-B’}] Algorithm to use for optimization. Only works at present with L-BFGS-B.

verbose [bool] Whether to print progress of model fitting

Returns

ModelFitResult Representation of the model fitting results

logposterior (*x, states, actions, rewards*)

Represents the log-posterior probability function

Parameters

x [ndarray(nparrays)] Array of parameters for single subject

states [ndarray] Array of states encountered by subject. Number of rows should reflect number of trials. If the task is a multi-step per trial task, then the number of columns should reflect the number of steps, unless a custom likelihood function is used which does not require this.

actions: ndarray Array of actions taken by subject. Number of rows should reflect number of trials. If the task is a multi-step per trial task, then the number of columns should reflect the number of steps, unless a custom likelihood function is used which does not require this.

rewards [ndarray] Array of rewards received by the subject. Number of rows should reflect number of trials. If there are multiple steps at which rewards are received, they should be stored in different columns, unless a custom likelihood funciton is used which does not require this.

Returns

float Log-posterior probability

Markov-Chain Monte-Carlo

```
class fitr.inference.mcmc.MCMC(generative_model=None, name='FitrMCMCModel')  
    Uses Markov-Chain Monte-Carlo (via PyStan) to estimate models
```

Attributes

- name** [str] Name of the model being fit
- generative_model** [GenerativeModel object]

Methods

<code>fit(self, data, chains=4, n_iterations=2000, warmup=None, thin=1, seed=None, init='random', sample_file=None, algorithm='NUTS', control=None, n_jobs=-1, compile_verbose=False, sampling_verbose=False)</code>	Runs the MCMC Inference procedure with Stan
<code>__initresults(self)</code>	(Private) method to initialize MCMC-FitResult object

```
fit (data, chains=4, n_iterations=2000, warmup=None, thin=1, seed=None, init='random', sample_file=None, algorithm='NUTS', control=None, n_jobs=-1, compile_verbose=False, sampling_verbose=False)  
Runs the MCMC Inference procedure with Stan
```

Parameters

- data** [dict] Subject level data
- chains** [int > 0] Number of chains in sampler
- n_iter** [int] How many iterations each chain should run (includes warmup)
- warmup** [int > 0, iter//2 by default] Number of warmup iterations.
- thin** [int > 0] Period for saving samples
- seed** [int or np.random.RandomState, optional] Positive integer to initialize random number generation
- sample_file** [str] File name specifying where samples for all parameters and other saved quantities will be written. If None, no samples will be written
- algorithm** [{‘NUTS’, ‘HMC’, ‘Fixed_param’}, optional] Which of Stan’s algorithms to implement
- control** [dict, optional] Dictionary of parameters to control sampler’s behaviour (see PyStan documentation for details)
- n_jobs** [int, optional] Sample in parallel. If -1, all CPU cores are used. If 1, no parallel computing is used
- compile_verbose** [bool] Whether to print output from model compilation
- sampling_verbose** [bool] Whether to print intermediate output from model sampling

Returns

- ModelFitResult** Instance containing model fitting results

References

[1]

Fitmodel: High Level Model-Fitting Wrapper

```
class fitr.inference.fitmodel.FitModel (name='Anon Model', loglik_func=None,  

params=None, generative_model=None)
```

An object representing a model to be fit to behavioural data. This should be viewed as a high level wrapper for multiple potential model fitting algorithms which themselves can be run by using their respective classes.

Attributes

- name** [str] Name of the model. We suggest identifying model based on free parameters.
- loglik_func** [function] The log-likelihood function to be used to fit the data
- params** [list] List of reinforcement learning parameter objects from the rlparams module.
- generative_model** [GenerativeModel object] Object representing a generative model

Methods

fit(data, method='EM', c_limit=0.01)	Runs the specified model fitting algorithm with the given data.
---	---

fit (*data, method='EM', c_limit=0.01, verbose=True*)

Runs model fitting

Parameters

- data** [dict] Behavioural data.
- method** [{‘EM’, ‘MLE’, ‘EmpiricalPriors’, ‘MCMC’}] The inference algorithm to use.
Note that the data formats for ‘MCMC’ compared to the other methods is distinct, and should correspond appropriately to the method being employed
- c_limit** [float] Limit at which convergence of log-posterior probability is determined (only for methods ‘EM’ and ‘EmpiricalPriors’)
- verbose** [bool] Controls amount of printed output during model fitting

Returns

fitrfit [object] Representation of the model fitting results

ModelFitResult

```
class fitr.inference.modelfitresult.MCMCFitResult (method, nsubjects, nparams, name)
```

Results of model fitting with MCMC

Attributes

- name** [str] Model identifier. We suggest using free-parameters as identifiers
- method** [str] Method employed in optimization.
- nsubjects** [int] Number of subjects fitted.
- nparams** [int] Number of free parameters in the fitted model.

params [ndarray(shape=(nsubjects, nparms))] Array of parameter estimates
paramnames [list] List of parameter names
stanfit Stan fit object
summary [pandas.DataFrame] Summary of the MCMC fit results

Methods

get_params estimates(self, FUN=np.mean)	Extracts parameter estimates
trace_plot(self, figsize=None, save_figure=False, filename='fitr-mcstan-traceplot.pdf')	Trace plot for fit results

get_params estimates(FUN=<Mock name='mock.median' id='140457368929488'>)
Extracts parameter estimates

Parameters

FUN [{numpy.mean, numpy.median}]

make_summary()

Creates summary of Stan fitting results

trace_plot(figsize=None, save_figure=False, filename='fitr-mcstan-traceplot.pdf')
Easy wrapper for Stan Traceplot

Parameters

figsize [(optional) list [width in inches, height in inches]] Controls figure size

save_figure [bool] Whether to save the figure to disk

filename [str] The file name to be output

class fitr.inference.modelfitresult.**ModelFitResult**(method, nsubjects, nparms,
name=None)

Class representing the results of a fitrmodel fitting.

Attributes

name [str] Model identifier. We suggest using free-parameters as identifiers

method [str] Method employed in optimization.

nsubjects [int] Number of subjects fitted.

nparms [int] Number of free parameters in the fitted model.

params [ndarray(shape=(nsubjects, nparms))] Array of parameter estimates

paramnames [list] List of parameter names

Methods

<code>set_paramnames(params)</code>	Sets names of RL parameters to the firfit object
<code>plot_ae(actual, save_figure=False, filename='actual-estimate.pdf')</code>	Plots estimated parameters against actual simulated parameters
<code>summary_table(write_csv=False, filename='summary-table.csv', delimiter=',')</code>	Writes a CSV file with summary statistics from the present model

ae_metrics (*actual*, *matches*=None)

Computes metrics summarizing the ability of the model to fit data generated from a known model

Parameters

matches [list] List consisting of [rlparams object, column index in *actual*, column index in estimates]. Ensures comparisons are being made between the same parameters, particularly when the models have different numbers of free parameters.

Returns

DataFrame Including summary statistics of the parameter matching

plot_ae (*actual*, *save_figure*=False, *filename*='actual-estimate.pdf')

Plots actual parameters (if provided) against estimates

Parameters

actual [ndarray(shape=(nsubjects, npars))] Array of actual parameters from a simulation

save_figure [bool] Whether to save the figure to disk

filename [str] The file name to be output

set_paramnames (*params*)

Sets the names of the RL parameters to the firfit object

Parameters

params [list] List of parameters from the rlparams module

class `fir.inference.modelfitresult.OptimizationFitResult` (*method*, *nsubjects*, *npars*, *name*)

Results of model fitting with optimization methods

Attributes

name [str] Model identifier. We suggest using free-parameters as identifiers

method [str] Method employed in optimization.

nsubjects [int] Number of subjects fitted.

npars [int] Number of free parameters in the fitted model.

params [ndarray(shape=(nsubjects, npars))] Array of parameter estimates

paramnames [list] List of parameter names

errs [ndarray(shape=(nsubjects, npars))] Array of parameter estimate errors

nlogpost [ndarray(shape=(nsubjects))] Subject level negative log-posterior probability

nloglik [float] Subject level negative log-likelihood

LME [float] Log-model evidence

BIC [ndarray(shape=(nsubjects))] Subject-level Bayesian Information Criterion

AIC [ndarray(shape=(nsubjects))] Subject-level Aikake Information Criterion

summary [DataFrame] Summary of means and standard deviations for each free parameter, as well as negative log-likelihood, log-model-evidence, BIC, and AIC for the model

Methods

plot_fit_ts(save_figure=False, filename='fit-stats.pdf')	Plots the evolution of log-likelihood, log-model-evidence, AIC, and BIC over optimization iterations
param_hist(save_figure=False, filename='param-hist.pdf')	Plots histograms of parameters in the model
summary_table(write_csv=False, filename='summary-table.csv', delimiter=',')	Writes a CSV file with summary statistics from the present model

param_hist (save_figure=False, filename='param-hist.pdf')

Plots histograms of the parameter estimates

Parameters

save_figure [bool] Whether to save the figure to disk

filename [str] The file name to be output

plot_fit_ts (save_figure=False, filename='fit-stats.pdf')

Plots the log-model-evidence, BIC, and AIC over optimization iterations

Parameters

save_figure [bool] Whether to save the figure to disk

filename [str] The file name to be output

summary_table()

Generates a table summarizing the model-fitting results

1.5.2 Model Selection

Modules:

Aikake Information Criterion Model-Selection

Bayesian Information Criterion Model-Selection

Bayesian Model Selection

Cross Validation Methods

Functions for cross validation

class fitr.criticism.cross_validation.**LOACV** (cv_func)

Look-one-ahead cross validation

Attributes

cv_func [loacv function] A look-one-ahead cross-validation function from a Fitr model

results [LookOneAheadCVResult] Stores results of the cross validation

Methods

<code>run</code> (params, data)	Runs the Look-One-Ahead cross validation
---------------------------------	--

run (*params, data*)
Runs the Look-One-Ahead cross validation

Parameters

params [ndarray(shape=(nsubjects, nparms))] Array of parameters

data [dict] Behavioural data in Fitr OptimizationData format

class fitr.criticism.cross_validation.**LookOneAheadCVResult** (*params*)
Stores and manipulates results of a Look-One-Ahead cross-validation run

Attributes

nsubjects [dict] Dictionary of

accuracy [dict] Dictionary of accuracy values (overall and by subject)

raw [dict] Dictionary

Methods

<code>accuracy_hist</code> ([<i>save_figure, filename, figsize</i>])	Plots moving average of accuracy
<code>accuracy_maplot</code> ([<i>save_figure, filename, figsize</i>])	Plots moving average of accuracy
<code>accuracy_param_scatter</code> ([<i>paramnames, ylim, ...</i>])	Plots accuracy against parameter values.

accuracy_hist (*save_figure=False, filename='accuracy-hist.pdf', figsize=None*)
Plots moving average of accuracy

Parameters

save_figure [bool] Whether to save the plot

filename [str] Name of the file to which figure will be saved

figsize [(optional) tuple (width, height)] The size of the figure

accuracy_maplot (*save_figure=False, filename='accuracy-maplot.pdf', figsize=None*)
Plots moving average of accuracy

Parameters

save_figure [bool] Whether to save the plot

filename [str] Name of the file to which figure will be saved

figsize [(optional) tuple (width, height)] The size of the figure

accuracy_param_scatter (*paramnames=None, ylim=None, alpha=0.5, save_figure=False, filename='accuracy-param-scatter.pdf', figsize=None*)
Plots accuracy against parameter values. Helpful to visually inspect the effects of various parameters on

cross-validation accuracy

Parameters

paramnames [(optional) list] List of parameter names in strings
ylim [(optional) tuple (min, max)] Y-axis limits
alpha [0 < float < 1] Transparency of the plot points
save_figure [bool] Whether to save the plot
filename [str] Name of the file to which figure will be saved
figsize [(optional) tuple (width, height)] The size of the figure

Returns

`matplotlib.pyplot.figure`

Model-Selection Result

class `fitr.criticism.modelselectionresult.ModelSelectionResult(method)`
Object containing results of model selection

Attributes

modelnames [list] List of strings labeling models
xp [ndarray] Exceedance probabilities for each model
pxp [ndarray] Protected exceedance probabilities for each model
BIC [ndarray] Bayesian information criterion measures for each model
AIC [ndarray] Aikake information criterion measures for each model

Methods

<code>plot(self, statistic, save_figure=False, filename='modelselection-plot.pdf', figsize=(10, 10))</code>	Plots the results of model selection (bars)
---	---

plot (`statistic, save_figure=False, filename='modelselection-plot.pdf', figsize=(10, 10)`)
Plots the results of model selection (bars)

Parameters

statistic [{‘pxp’, ‘xp’, ‘BIC’, ‘AIC’}] Which statistic is desired for the bar plot
save_figure [bool] Whether to save the figure
filename [str] The desired filename for the plot (must end in appropriate extension)
figsize [tuple, default (10, 10)]

1.5.3 Task Models and Data Objects

Modules:

Synthetic Data

```
class fitr.models.synthetic_data.SyntheticData
Object representing synthetic data
```

Attributes

- data** [dict] Dictionary containing data formatted for fitr's model fitting tools (except MCMC via Stan)
- data_mcmc** [dict] Dictionary containing task data formatted for use with MCMC via Stan
- params** [ndarray(shape=(nsubjects X nparms))] Subject parameters
- groupnames** [list] Strings representing names of groups whose data are represented

Methods

append_group(self, data=SyntheticData)	
get_nparams(self)	Returns the number of parameters in the data
get_nsubjects(self)	Returns the number of subjects in the data
cumreward_param_plot(self, alpha=0.9)	Plots the cumulative reward against model parameters. Useful to determine the relationship between reward acquisition and model parameters for a given task.
plot_cumreward(self)	Plots the cumulative reward over time for each subject

append_group (data, which='all')

Appends data from other groups to the SyntheticData object

Parameters

data [SyntheticData object]

all [{‘all’, ‘opt’, ‘mcmc’}] Whether to append all data, optimization data only, or MCMC data

cumreward_param_plot (alpha=0.9, save_figure=False, filename='cumreward-param-plot-sim.pdf')

Plots parameter values against cumulative reward

Parameters

save_figure [bool] Whether to save the figure to disk

filename [str] The name of the file to which to save the figure

get_nparams()

Finds the number of parameters in the model

Returns

int

get_nsubjects()

Finds the number of subjects in the data

Returns

int

```
plot_cumreward(save_figure=False, filename='cumreward-plot-sim.pdf')
```

Plots cumulative reward over time for each subject

Parameters

save_figure [bool] Whether to save the figure to disk

filename [str] The name of the file to which to save the figure

```
fitr.models.synthetic_data.combine_groups(x, y)
```

Combines synthetic data objects for multiple groups

Parameters

x [SyntheticData] Data for first simulated group

y [SyntheticData] Data for second simulated group

Returns

SyntheticData Combined groups

1.5.4 Plotting Functions

Modules:

Distance Metric Plots

Plotting functions for distance metrics

Module Documentation

```
fitr.plotting.distance.distance_hist(X, group_labels, xlab='Distance', ylab='', normed=1, alpha=0.5, save_figure=False, figsize=None, fname='distance-hist.pdf')
```

Creates a histogram of within- and between-group distances.

Parameters

group_labels [ndarray(size=n_labels)] Vector of group labels for each participant represented

xlab [str] X-axis label

ylab [str] Y-axis label

normed [0 or 1 (default=1)] Whether the histogram should be normalized

alpha [float on interval (0, 1)] Transparency of scatterplot points

save_figure [bool] Whether to save the figure

figsize [(optional) list] Controls figure size

fname [str] The name under which the plot should be saved

```
fitr.plotting.distance.distance_scatter(X, Y, group_labels=None, xlab='', ylab='', alpha=0.5, save_figure=False, figsize=None, fname='distance-scatter.pdf')
```

Creates a scatterplot between two distance metrics, demonstrating group separation, if any.

Parameters

```
group_labels [(optional)]
xlab [str] X-axis label
ylab [str] Y-axis label
alpha [float on interval (0, 1)] Transparency of scatterplot points
save_figure [bool] Whether to save the figure
figsize [(optional) list] Controls figure size
filename [str] The name under which the plot should be saved
```

ParamPlots

Various plotting functions for parameter estimates

Module Documentation

```
fitr.plotting.paramplots.param_scatter(X, paramnames=None, xlabel='Parameter Value',
                                         ylabel='y value', ylim=None, alpha=0.5, figsize=None,
                                         save_figure=False, filename='param-
                                         scatter.pdf')
```

Plots a value against parameter estimates for each parameter

Parameters

```
X [ndarray(shape=(nsubjects, nparams))] Parameter array
Y [ndarray(shape=nsubjects)] Value to be plotted against parameters
paramnames [(optional) list] Parameter names (will be the title for each plot)
xlabel [str] Label for x axis
ylabel [str] Label for y axis
ylim [(optional) tuple (min, max)] Y-axis limits
alpha [0 < float < 1] Transparency of scatter points
figsize [(optional) tuple (width, height)]
save_figure [bool] Whether to save the plot
filename [str] Path to which to plot the figure
```

Returns

```
matplotlib.pyplot.figure
```

1.5.5 RLParams

Module containing commonly used reinforcement learning parameter objects.

Module Documentation

```
class fitr.rlparams.ChoiceRandomness(name='Choice Randomness', rng='pos', mean=4, sd=1)
```

An choice randomness parameter object

Attributes

name [str] Name of the parameter. To be used for plots and so forth.

rng [{‘unit’, ‘pos’, ‘neg’, ‘unc’}] The domain over which the parameter lies (unit=[0,1], pos=[0,+Inf], neg=[-Inf,0], unc=[-Inf, +Inf])

dist [scipy.stats.gamma distribution]

Methods

sample(size=1)	Samples from the parameter’s distribution
-----------------------	---

```
class fitr.rlparams.EligibilityTrace(name='Eligibility Trace', rng='unit', mean=0.5, sd=0.27)
```

An eligibility trace parameter object.

Attributes

name [str] Name of the parameter. To be used for plots and so forth.

rng [{‘unit’, ‘pos’, ‘neg’, ‘unc’}] The domain over which the parameter lies (unit=[0,1], pos=[0,+Inf], neg=[-Inf,0], unc=[-Inf, +Inf])

dist [scipy.stats.beta distribution]

Methods

sample(size=1)	Samples from the parameter’s distribution
-----------------------	---

```
class fitr.rlparams.LearningRate(name='Learning Rate', rng='unit', mean=0.5, sd=0.27)
```

A learning rate object.

Attributes

name [str] Name of the parameter. To be used for plots and so forth.

rng [{‘unit’, ‘pos’, ‘neg’, ‘unc’}] The domain over which the parameter lies (unit=[0,1], pos=[0,+Inf], neg=[-Inf,0], unc=[-Inf, +Inf])

dist [scipy.stats.beta distribution]

Methods

sample(size=1)	Samples from the parameter’s distribution
-----------------------	---

```
class fitr.rlparams.MBMF_Balance(name='Model-Based Control Weight', rng='unit', mean=0.5, sd=0.27)
```

An object representing the parameter that balances model-based and model-free control.

Attributes

name [str] Name of the parameter. To be used for plots and so forth.

rng [{‘unit’, ‘pos’, ‘neg’, ‘unc’}] The domain over which the parameter lies (unit=[0,1], pos=[0,+Inf], neg=[-Inf,0], unc=[-Inf, +Inf])

dist [scipy.stats.beta distribution]

Methods

sample(size=1)	Samples from the parameter’s distribution
-----------------------	---

class fitr.rlparams.**Param**(name=None, rng=None)

A base parameter object that can be used to generate new parameters.

Attributes

name [str] Name of the parameter. To be used for plots and so forth.

rng [{‘unit’, ‘pos’, ‘neg’, ‘unc’}] The domain over which the parameter lies (unit=[0,1], pos=[0,+Inf], neg=[-Inf,0], unc=[-Inf, +Inf])

Methods

sample(size=1)	Samples from the parameter’s distribution
-----------------------	---

convert_meansd(mean, sd, dist)

Converts mean and standard deviation to other distribution parameters.

Parameters

mean [float] Mean value for distribution (must lie within region of support)

sd [float] Standard deviation for distribution

dist [{‘beta’, ‘gamma’}] Target distribution

Notes

Currently, only the gamma and beta distributions are supported for this function.

The Beta distribution has two shape parameters $\{\alpha, \beta\} > 0$. Using the mean μ and the standard deviation σ , the α parameter can be calculated as

$$\alpha = \left(\frac{1 - \mu}{\sigma^2} - \frac{1}{\mu} \right) \mu^2$$

and the β parameter as

$$\beta = \alpha \left(\frac{1}{\mu} - 1 \right)$$

Note that for the Beta distribution to be defined this way, the following constraint must hold for the mean, $0 < \mu < 1$, and the following for the variance, $0 < \sigma^2 \leq \mu - \mu^2$.

For the Gamma distribution, we have a shape parameter $\kappa > 0$ and a scale parameter θ . These can be calculated using the mean μ and standard deviation σ as

$$\theta = \frac{\sigma^2}{\mu}$$

and

$$\kappa = \frac{\mu^2}{\sigma^2}$$

plot_pdf (*xlim=None*, *figsize=None*, *save_figure=False*, *filename='parameter-pdf.pdf'*)
Plots the probability density function of this parameter

Parameters

xlim [(optional) list of lower and upper bounds of x axis]
figsize [(optional) list defining plot dimensions]
save_figure [bool] Whether to save the figure at function call
filename [str] The name of the file at which to save the figure

sample (*size=1*)

Samples from the parameter's distribution

Parameters

size [int] Number of samples to draw

Returns

ndarray

class fitr.rlparams.**Perseveration** (*name='Perseveration'*, *rng='unc'*, *mean=0.0*, *sd=0.1*)
An perseveration parameter object

Attributes

name [str] Name of the parameter. To be used for plots and so forth.
rng [{‘unit’, ‘pos’, ‘neg’, ‘unc’}] The domain over which the parameter lies (unit=[0,1], pos=[0,+Inf], neg=[-Inf,0], unc=[-Inf, +Inf])
dist [scipy.stats.norm distribution]

Methods

sample(size=1)	Samples from the parameter's distribution
-----------------------	---

class fitr.rlparams.**RewardSensitivity** (*name='Reward Sensitivity'*, *rng='unit'*, *mean=0.5*, *sd=0.27*)
A reward sensitivity object.

Attributes

name [str] Name of the parameter. To be used for plots and so forth.
rng [{‘unit’, ‘pos’, ‘neg’, ‘unc’}] The domain over which the parameter lies (unit=[0,1], pos=[0,+Inf], neg=[-Inf,0], unc=[-Inf, +Inf])
dist [scipy.stats.beta distribution]

Methods

<code>sample(size=1)</code>	Samples from the parameter's distribution
-----------------------------	---

1.5.6 Utils

Module containing functions that are used across Fitr modules

References

Module Documentation

`fitr.utils.action(x)`

Selects an action based on state-action values

Parameters

`x` [ndarray] Array of action values (scaled by inverse softmax temperature).

Returns

`int` The index corresponding to the selected action

Notes

This function computes the softmax probability for each action in the input array, and subsequently samples from a multinomial distribution parameterized by the results of the softmax computation. Finally, it returns the index where the value is equal to 1 (i.e. which action was selected).

`fitr.utils.logsumexp(x)`

Numerically stable logsumexp.

Parameters

`x` [ndarray(shape=(nactions))]

Returns

`float`

Notes

The numerically stable log-sum-exp is computed as follows:

$$\max X + \log \sum_X e^{X - \max X}$$

`fitr.utils.softmax(x)`

Computes numerically stable softmax

Parameters

`x` [ndarray(shape=(nactions))]

Returns

`ndarray(shape=(nactions))` Softmax probabilities for each action

`fitr.utils.trans_UC(values_U, rng)`
Transforms parameters from unconstrained to constrained space

Parameters

`values_U` [ndarray] Parameter values
`rng` [{‘unit’, ‘pos’, ‘half’, ‘all_unc’ }] The constrained range of the parameter

Returns

`ndarray(shape=(nparams))`

Notes

This code was taken from that published along with [Akam2015].

CHAPTER 2

Overview

In decision-making tasks, it is often of interest to understand the psychological mechanisms by which a subject makes choices. One way to approach this problem is by specifying a reinforcement learning (RL) model that describes those mechanisms, and then fitting it (by tuning its free parameters) to subjects' actual behavioural data. There are many ways to perform this analysis, which for the most part might be inaccessible to researchers without extensive mathematical training. We are building Fitr as an attempt to make this process simpler to implement.

For researchers interested in the computational aspects of decision-making research, Fitr also aims to offer pre-packaged routines to streamline the study & development of new tasks, models, and model-fitting/selection procedures.

CHAPTER 3

Goals

1. **Offer a free and open platform upon which researchers can easily**
 - Build and validate behavioural tasks
 - Build and validate behavioural models
 - Develop new model-fitting procedures
 - Fit models to behavioural data from subjects *in vivo*
2. Implement the state of the art methods for behavioural modelling studies in computational psychiatry
3. Integrate well with tools for collecting behavioural data
4. Integrate well with tools for collecting neurophysiological data

CHAPTER 4

Guiding Principles

1. Accessibility

- Fitr should be open-source, free, and not dependent on commercial tools

2. Parsimony

- Build tools that can turn data into results with minimal coding

3. Modularity

- **Build modules, classes, and functions in a way that facilitates the computational modelling workflow as it applies to:**
 - Developing and validating tasks
 - Developing and validating models
 - Fitting/selecting models using data from human subjects

4. Flexibility

- There are many ways to fit a model. Users should be able to easily test multiple models and multiple fitting methods without much additional code.
- Allow users to easily integrate their own code, where desired
- Facilitate development of “Pipelines” for Computational Psychiatry research

5. Don’t re-invent the wheel (unless you have to)

- If excellent open-source tools exist, don’t rebuild them. Rather, make it possible for users to integrate them easily into their workflow
- Always give credit wherever credit is due

6. Build for communication and reproducibility

- Make it easy for researchers to generate the high-quality tables and plots necessary to communicate the results of their modelling studies.
- Make it easy to reproduce results generated by Fitr pipelines

CHAPTER 5

What we're working on

- Adding new tasks and new models
- Writing more tutorials
- End-to-end model-fitting and model-selection
- Improving existing model-fitting algorithms
- Adding new model-fitting algorithms (Variational Bayes)
- Model-based neuroimaging

CHAPTER 6

Citing Fitr

Let us know if you publish a paper using Fitr and we will post it here. If you use Fitr in your work, please cite it so that we can (A) know how people have been using it, and (B) support further funding of our work.

- Abraham Nunes, Alexander Rudiuk, & Thomas Trappenberg. (2017). Fitr: A Toolbox for Computational Psychiatry Research. Zenodo. <http://doi.org/10.5281/zenodo.439989>

CHAPTER 7

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